TRAJECTORY TRACKING CONTROLLER DESIGN FOR QUADCOPTER UNDER DISTURBANCES ENVIRONMENT: USING A HYBRID APPROACH

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Abstract

The development of a robust tracking controller for autonomous aerial vehicles to reach the desired point has become extremely important, especially when flying in the ground region. This paper proposes a hybrid controller (proportional fractional-order integral derivative sliding surface based on sliding mode control with backstepping (PFOIDSMCBS)) to control the quadcopter to flow the predefined trajectory. The proposed controller is designed to control the attitude, altitude, and angular motion with payload in the presence of external disturbances, wind, and ground effects. The performances of the proposed controller have been compared with the existing SMCBS controller. The simulation results show that the system satisfies the stability condition and is efficient in path tracking. As the vehicle approaches the ground, the simulation indicates a consistent linear increase in the total thrust generated by the rotors. In the landing, the proposed controller reduces settling time by 6.12% compared to SMCBS for the system without load. With a load, it reduces settling time by 5.17% compared to SMCBS. PFOIDSMCBS controller exhibits superior performance over SMCBS in terms of minimizing chattering effects and reducing control effort.

Key words

Quadcopter model, Nonlinear system, Hybrid controller.

1 Introduction

Quadcopters, unmanned aerial vehicles, have attracted significant attention due to their numerous applications [Yacef et al., 2014; Araar and Aouf, 2014]. The quadcopter system an under-actuated system possesses six degrees of freedom (DoF) while having only four control inputs, due to this quadcopters require effective flight control, especially during takeoff, inflight, and landing. The takeoff and landing of quadcopters on the ground surface or any surface have been discussed by many authors [Kumar and Dewan, 2024; Danjun et al., 2015]. Most of the work has been focused on ensuring the quadcopter's safe landing on its target. During flight, as the quadcopter enters or exits the ground effect region, it impacts due to this ground effect. In [Fujita and Shimada, 2007] author has derived equations for the ground effect and provided a methodology to calculate how it influences the quadcopter. First, in 1957, Cheeseman's model derivation the thrust ratio inside and outside the ground effect for a single-rotor helicopter, after that other authors gave the modified Cheeseman's model calculation [Davis et al., 2015]. In [Danjun et al., 2015] author, clarify the behavior of the ground effect on the helicopter as well as quadcopter. Various aspects of the ground effect have been addressed experimentally, mathematically, and computationally by the authors [Sharf et al., 2014]. Quadcopters are also sensitive to wind gusts, which affect the control of the quadcopter and make it dangerous to operate in populated areas. However, there is less research quantifying the wind effects. The literature [Chen et al., 2013; Waslander and Wang, 2009] explains that wind effects increase due to the wind flow interaction with the propellers. Wind gusts taken as a disturbance force vector has been given by [Dikmen et al., 2009; Tran et al., 2015], and the addition of a dynamic wind model in a state-space model of the quadcopter has been represented in [Ambati and Padhi, 2014; Nekoo et al., 2021]. The payload acts as a mass variation of the quadcopter resulting in a loss of commandability. As fuel constitutes a considerable portion of the vehicle's total mass, this problem becomes more apparent [Cho et al., 2020].

Safety, operational reliability, predefined path trajectory tracking, and controlling of the quadcopters have been represented by many researchers in our work [Mori et al., 2008; Watanabe et al., 2008]. Most of the time, linear and nonlinear controllers have been designed by authors to control the performance of the quadcopter [Kumar and Dewan, 2020; Sharma and Lather, 2020]. Different nonlinear controllers have been proposed to address the external disturbances [Sadeghzadeh et al., 2014], wind effect [Ambati and Padhi, 2014], atmospheric disturbances [Alexis et al., 2011], and timeinvariant disturbances in [Cho et al., 2020], [Gao and Wang, 2013]. Other control techniques, such as hybrid control [Sahrir and Basri, 2023], [Kumar and Dewan, 2022], have been proposed to mitigate the effect of sensor noise, wind as a shock, external disturbances, and mass variation, etc. In addition, by applying the principles of fractional calculus, the efficacy of sliding mode control (SMC) is improved by the combination of the advantages of both theories. In recent years, there has been various research that has expanded the application of fractional order sliding mode control (FOSMC) to tackle disturbances and uncertainties in quadrotor control. In [Ayad et al., 2019], a continuous-time fractionalorder proportional-derivative (PD) controller was introduced. A fractional-order sliding mode controller, utilizing backstepping, has been introduced [Vahdanipour and Khodabandeh, 2019] to alleviate wind disturbances and fluctuations in load moment of inertia. Similarly, a new fractional-order proportional-integral (PI) nonlinear system for quadrotor attitude control was proposed by [Oliva-Palomo et al., 2019]. The authors [Hua et al., 2019] developed a controller based on fractional-order sliding mode theory to address the tracking issue of an uncertain quadrotor with time-varying state constraints.

A model of quadcopter [Bouabdallah and Siegwart, 2005] has been used for the development of the control system. In this paper, an effort has been made to enhance this model by adding various disturbances, aiming to achieve a more comprehensive dynamic model to [Xiong and Zheng, 2014]. This paper design a novel controller that combines the advantages of SMCBS with fractional theory to develop a fractional order of ID (PFOID) for controlling a quadcopter in the presence of uncertain parameters and external disturbances. Using the proposed controller the system's capacity to achieve fast-tracking performance and accurate control over attitude and position is improved. To emphasize the effectiveness of the proposed controller, a comparison evaluation is performed with existing controllers SMCBS [Thanh and Hong, 2018]. The comparison demonstrates that the proposed strategy outperforms in trajectory tracking. Drawing motivation from the aforementioned works, the following is an overview of the key contributions of this article;

Proposes a novel sliding mode control (SMC) with backstepping (BS) based on a proportional fractionalorder integral derivative (PFOID) sliding surface controller that successfully controls a quadcopter in the presence of uncertainties and disturbances. The primary goal of this controller is to effectively counteract and eliminate external disturbances (aerodynamic effect, sensor noise, external disturbance, wind effect, ground effect, and payload). By applying the proposed controller (PFOIDSMCBS), improved performance specifications are achieved, including faster settling time, low overshoot, reduced error, and minimized chattering effects compared to the SMCBS controller [Thanh and Hong, 2018]. Implementation of the proposed controller allows the quadcopter to achieve the desired trajectory with more accuracy, superior performance compared to the existing controllers, and the ability to effectively reduce tracking issues. The stability conditions of the system have been derived using Lyapunov stability criteria. Simulation scenarios were designed with high realism, aligning them closely with real-world applications such as transportation, agricultural spraying, etc.

The layout of the paper is as outlined: Section 1 starts with a brief overview, and Section 2 presents the quadcopter's dynamics, taking into account the wind and ground effects. Derivation of the controller and Lyapunov stability concept are given in Section 3, followed by implementation in Section 4, and Conclusion in Section 5.

2 Quadcopter Mathematical Modelling

2.1 Quadcopter Model

The section describes the quadcopter dynamics model [Kumar and Dewan, 2023]. The structure of the quadcopter is shown in Fig. 1, with their earth and body frames, as well as the rotational and translational motion directions.

This paper considers Φ , θ , and ψ (roll, pitch, and yaw) to be the angles of the quadcopter. The positions of the quadcopter are denoted by x, y, and z, and j_{xx} , j_{yy} , j_{zz} represent the relative inertial moments along the x, y, and z axes, respectively.

The linear and angular velocities of the body frame (B_f) are denoted as;

$$v_l = [u_l, v_l, w_l]^T \quad (\text{m/s}),$$

$$v_r = [u_r, v_r, w_r]^T \quad (\text{rad/s})$$

This section describes a transformation matrix \mathbf{M}_{tra} and a rotational matrix \mathbf{M}_{rot} from the body frame (B_f) to the earth frame (E_f) and vice versa using the Euler angles method. This method, introduced by Leonhard Euler, is well-understood and easy to implement.

The rotational matrices for the roll (Φ), pitch (θ), and yaw (ψ) angles are defined as follows:

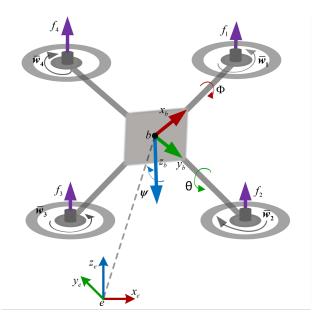


Figure 1. Quadcopter Model

$$\begin{split} \mathbf{M}_{\text{rotx}}(\Phi) &= \begin{bmatrix} 1 & 0 & 0 \\ 0 \cos(\Phi) & -\sin(\Phi) \\ 0 \sin(\Phi) & \cos(\Phi) \end{bmatrix}, \\ \mathbf{M}_{\text{roty}}(\theta) &= \begin{bmatrix} \cos(\theta) & 0 \sin(\theta) \\ 0 & 1 & 0 \\ -\sin(\theta) & 0 \cos(\theta) \end{bmatrix}, \\ \mathbf{M}_{\text{rotz}}(\psi) &= \begin{bmatrix} \cos(\psi) & -\sin(\psi) & 0 \\ \sin(\psi) & \cos(\psi) & 0 \\ 0 & 0 & 1 \end{bmatrix}. \end{split}$$

The rotation and transformation matrix from the body frame (B_f) to the earth frame (E_f) is defined as:

$$\mathbf{M}_{\text{rot}} = \mathbf{M}_{\text{rot}}(\psi, \theta, \Phi)$$
$$= \begin{bmatrix} c_{\theta}c_{\psi} \ s_{\Phi}s_{\theta}c_{\psi} - c_{\Phi}s_{\psi} \ c_{\Phi}s_{\theta}c_{\psi} + s_{\Phi}s_{\psi} \\ c_{\theta}s_{\psi} \ s_{\Phi}s_{\theta}s_{\psi} + c_{\Phi}c_{\psi} \ c_{\Phi}s_{\theta}s_{\psi} - s_{\Phi}c_{\psi} \\ -s_{\theta} \ s_{\Phi}c_{\theta} \ c_{\Phi}c_{\theta} \end{bmatrix}$$
(1)

The transformation matrix is defined as:

$$\mathbf{M}_{\text{tra}} = \begin{bmatrix} 1 \ s_{\Phi} t_{\theta} \ c_{\Phi} t_{\theta} \\ 0 \ c_{\Phi} \ -s_{\Phi} \\ 0 \ \frac{s_{\Phi}}{c_{\theta}} \ \frac{c_{\Phi}}{c_{\theta}} \end{bmatrix}$$

Here, $s = \sin$, $c = \cos$, and $t = \tan$. Therefore, the dynamics are described using the Newton-Euler equations as follows [Nekoo et al., 2021]:

$$m(\mathbf{v}_r \times \mathbf{v}_l + \dot{\mathbf{v}}_l) = F_B - mgM_{\text{tra}}c_3 \qquad (2)$$

$$\dot{\mathbf{v}}_{l} = \begin{bmatrix} \dot{u}_{l} \\ \dot{v}_{l} \\ \dot{w}_{l} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \frac{\eta_{B}}{m} \end{bmatrix} \begin{bmatrix} 0 & -w_{r} & v_{r} \\ w_{r} & c_{\Phi} & -u_{r} \\ -v_{r} & u_{r} & 0 \end{bmatrix} \begin{bmatrix} u_{l} \\ v_{l} \\ w_{l} \end{bmatrix} -g \begin{bmatrix} -s_{\theta} \\ c_{\theta}s_{\Phi} \\ c_{\theta}c_{\pi} \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

Considered in the hover state, the rotation of the body coordinate relative to the inertial frame; therefore, it is approximated that

$$\dot{\mathbf{M}}_{\mathrm{rot}}\mathbf{v}_l + \mathbf{M}_{\mathrm{rot}}\dot{\mathbf{v}}_l \approx \dot{\mathbf{v}}_l.$$

Then, the gravity and \mathbf{F}_B are transformed into the body frame B_f .

The equation for $\dot{\mathbf{v}}_l$ is given by:

$$\dot{\mathbf{v}}_{l} = \begin{bmatrix} \dot{u}_{l} \\ \dot{v}_{l} \\ \dot{w}_{l} \end{bmatrix} = \begin{bmatrix} c_{\Phi}s_{\theta}c_{\psi} + s_{\Phi}s_{\psi} \\ c_{\Phi}s_{\theta}c_{\psi} - s_{\Phi}c_{\psi} \end{bmatrix} \frac{\tau_{B}}{m} \\ - \begin{bmatrix} 0 & -w_{r} & v_{r} \\ w_{r} & c_{\Phi} - u_{r} \\ -v_{r} & u_{r} & 0 \end{bmatrix} \begin{bmatrix} u_{l} \\ v_{l} \\ w_{l} \end{bmatrix} - \begin{bmatrix} 0 \\ 0 \\ g \end{bmatrix} \\ - \frac{1}{m} \begin{bmatrix} j_{xx} & 0 & 0 \\ 0 & j_{yy} & 0 \\ 0 & 0 & j_{zz} \end{bmatrix} \begin{bmatrix} \dot{x}_{B} \\ \dot{y}_{B} \\ \dot{z}_{B} \end{bmatrix}$$
(3)

$$\hat{\mathbf{v}}_{\text{rot}} = \begin{bmatrix} 0 & -w_r & v_r \\ w_r & 0 & -u_r \\ -v_r & u_r & 0 \end{bmatrix}$$

$$\mathbf{j} = \operatorname{diag}(j_{xx}, j_{yy}, j_{zz})$$

 τ_B : Thrust of the propeller in ground effect, \mathbf{F}_B : Input force vector.

In the body frame, the rotational dynamic is:

$$\mathbf{j}\dot{\mathbf{v}}_{rot} + \mathbf{v}_{rot} \times \mathbf{j}\mathbf{v}_{rot} = \mathbf{u}_B$$

where \mathbf{j} is the identity matrix.

$$\dot{\mathbf{v}}_{r} = \begin{bmatrix} \dot{u}_{r} \\ \dot{v}_{r} \\ \dot{w}_{r} \end{bmatrix} = \begin{bmatrix} \frac{I_{\Phi}}{j_{\bar{x}x}} \\ \frac{I_{\theta}}{j_{yy}} \\ \frac{I_{\psi}}{j_{zz}} \end{bmatrix}$$
$$-\mathbf{j}^{-1} \begin{bmatrix} 0 & -w_{r} & v_{r} \\ w_{r} & c_{\Phi} & -u_{r} \\ -v_{r} & u_{r} & 0 \end{bmatrix} \begin{bmatrix} j_{xx} & 0 & 0 \\ 0 & j_{yy} & 0 \\ 0 & 0 & j_{zz} \end{bmatrix} \begin{bmatrix} u_{r} \\ v_{r} \\ w_{r} \end{bmatrix}$$
(4)

Using the 4 rotors, thrust and moment are produced in the quadcopter's with rotating at an angular speed $\bar{\omega}(t)$ (rad/s). So, the angular velocity of the rotors is:

$$\bar{\omega}(t) = \sqrt{\left(\begin{bmatrix} k & k & k & k \\ 0 & -lk & 0 & k \\ -lk & 0 & lk & 0 \\ -K_c & K_c & -K_c & K_c \end{bmatrix}^{-1} \begin{bmatrix} I_z \\ I_{\Phi} \\ I_{\theta} \\ I_{\psi} \end{bmatrix} \right)}$$
(5)

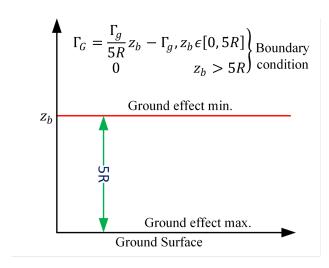


Figure 2. Ground effect region

2.2 Ground modelling

In the flight stage, the quadcopter approaches the surface (near the landing), and the thrust is turned off. Then, the quadcopter loses its controllability and drops to the surface. Therefore, quadcopter landing time is not guaranteed. For a quadcopter to land on a fixed point, the accuracy of the landing time is crucial.

The ground effect equation derived in [Sanchez-Cuevas et al., 2017] with a relation for calculating thrust close to the ground;

$$\frac{\tau_g}{\tau_B} = \frac{1}{1 - \left(\frac{R}{4z_b}\right)^2 - \frac{R^2 z_b}{\sqrt{(d+4z_b^2)^3}} - \frac{R^2 z_b}{\sqrt{2(2d+4z_b^2)^3}}} \quad (6)$$

$$\tau_g = 2\rho A_o \Gamma_g^2, \quad \tau_B = 2\rho A_o \Gamma_o^2$$

Eq. (6) represents the ground reflection of wind with direction towards the ground -z, thus the negative sign for Γ_g :

$$\frac{\tau_g}{\tau_B} = \frac{1}{1 - \left(\frac{R}{4z_b}\right)^2 - \frac{R^2 z_b}{\sqrt{(d+4z_b^2)^3}} - \frac{R^2 z_b}{\sqrt{2(2d+4z_b^2)^3}}}$$
(7)

There will be some wind loss due to turbulence and interference of the airflows by rotors, though the maximum reflection $\Gamma_G \leq \Gamma_g$ is always less than Γ_g . Therefore, the controller design based on Eq. (7) is safe and covers the ground wind reaction since Γ_g , in reality, is less than the theoretical design.

 τ_q : Thrust of propeller outside ground effect, Γ_o : Air

velocity far from the ground, Γ_g : Air velocity near to the ground, Γ_G : Air velocity reflected to the ground.

Figure 2 represents the maximum and minimum region of ground effect with boundary conditions. To achieve a smooth and soft landing without relying on specialized landing gear, it's essential to account for the wind reflection generated by the ground in the controller design and system modeling.

2.3 Wind Modelling

Wind velocity coordinates of the quadcopter are defined as $\bar{\mathbf{w}} = \begin{bmatrix} w_x \ w_y \ w_z \end{bmatrix}^T$ (m/s) [Nekoo et al., 2021]. Transforming the wind coordinate to the body frame of the quadcopter, the translation matrix is:

$$\bar{\mathbf{w}}(t) = d_i^w = \begin{bmatrix} w_x \ w_y \ w_z \end{bmatrix}^T = R_{zxy}^T(r_2)\mathbf{w} \quad (8)$$

$$\bar{\mathbf{w}}(t) = \begin{bmatrix} 0 \ 0 \ \Gamma_G(t) \end{bmatrix} \quad [\text{Lungu}, 2020], \quad (9)$$

for a soft landing of the quadcopter on the ground.

2.4 Disturbances

The robustness of the controller was verified by adding various disturbances to the quadcopter's dynamic: aerodynamic effect d_i^a (i.e., $\sin(2t)$); random noise d_i^s is added as random noise (lie 0 to 1); external disturbance d_i^e [Kumar and Dewan, 2023] are defined as:

$$\begin{bmatrix} d_{\phi}^{en}(t) = d_{\theta}^{en}(t) = 7 + 2\cos\left(\frac{2\pi}{3}t\right), \\ d_{\psi}^{en}(t) = 5 + 2\cos\left(\frac{\pi}{2}t\right), \\ d_{x}^{en}(t) = d_{y}^{en}(t) = d_{z}^{en}(t) = 18 + 4\cos\left(\frac{\pi}{6}t\right) \end{bmatrix}$$

Total external disturbances written as:

Translation motion;

$$d_{\rm tri} = d_i^a + d_i^s + d_i^e + d_i^{pu} + d_i^w$$

where i = x, y, z. Rotational motion:

$$d_{\rm roi} = d_i^a + d_i^s + d_i^e + d_i^{pu} + d_i^w \qquad (10)$$

where $i = \Phi, \theta, \psi$. Furthermore, parametric uncertainties were added to the system. This represents a 20% mass variation that can be included in the landing load drop and hovering dynamics.

3 Controller design

This section introduces a controller design that addresses the control of the quadcopter rotation and translation motion in the presence of model uncertainties and disturbances. The quadcopter dynamics are nonlinear and underactuated because it has 4

Parameters	Name	Value/Unit				
m	Mass	0.23 kg				
$j_{xx} = j_{yy}$	Moment of inertia in	7.5×10^(-3) kgm^2				
	the x and y-axis	7.5×10 (-5) kgili 2				
j_{zz}	Moment of inertia in	$1.2 \times 10^{2} (2) \text{ kmm}^{2}$				
	the z-axis	1.3×10^(-2) kgm ²				
Ω_r	Rotor inertia	6×10^(-2) kgm^2				
k	Thrust coefficient	3.13×10^(-5)				
	Thrust coefficient	Nms^2				
,	Drag Coofficient	7.5×10^(-7)				
k_c	Drag Coefficient	Nms ²				
1	Length	0.23 m				
R	Radius of the	0.075 m				
	propellers	0.075 III				
A_o	Air density	1.225km/m^3				

Table 1. Physical Parameters

control inputs $(I_z, I_{\Phi}, I_{\theta}, I_{\psi})$ and 6 outputs $(x, y, z, \Phi, \theta, \psi)$.

The state-space form representation of the dynamic model of the quadcopter is [Kumar and Dewan, 2023]:

$$\dot{X} = f(X, u) + d(X, u)$$

where X, d, and u are the state, disturbances, and input vectors, respectively.

$$X = \begin{bmatrix} x_1 & x_2 & x_3 & x_4 & x_5 & x_6 & x_7 & x_8 & x_9 & x_{10} \\ x_{11} & x_{12} \end{bmatrix}^T$$
$$= \begin{bmatrix} \Phi & \dot{\Phi} & \theta & \dot{\theta} & \psi & \dot{\psi} & z & \dot{z} & x & \dot{x} \\ y & \dot{y} & & \end{bmatrix}^T \in \mathbb{R}^{12}$$

$$\dot{X} = \begin{bmatrix} \dot{x}_{1} = \dot{\Phi} = x_{2} \\ \dot{x}_{2} = \ddot{\Phi} = a_{1}\dot{\theta}\dot{\psi} + a_{2}\ddot{\theta}\Omega_{r} + b_{\Phi}I_{\Phi} + d_{ro\Phi} \\ \dot{x}_{3} = \dot{\theta} = x_{4} \\ \dot{x}_{4} = \ddot{\theta} = a_{3}\dot{\psi}\dot{\Phi} + a_{4}\ddot{\Phi}\Omega_{r} + b_{\theta}I_{\theta} + d_{ro\theta} \\ \dot{x}_{5} = \dot{\psi} = x_{6} \\ \dot{x}_{6} = \ddot{\psi} = a_{5}\dot{\Phi}\dot{\theta} + b_{\psi}I_{\psi} + d_{ro\psi} \\ \dot{x}_{7} = \dot{z} = x_{8} \\ \dot{x}_{8} = \ddot{z} = -g + (\delta_{z})\frac{I_{z}}{m} + d_{roz} \\ \dot{x}_{9} = \dot{x} = x_{10} \\ \dot{x}_{10} = \ddot{x} = (\delta_{x})\frac{I_{x}}{m} + d_{rox} \\ \dot{x}_{11} = \dot{y} = x_{12} \\ \dot{x}_{12} = \ddot{y} = (\delta_{y})\frac{I_{y}}{m} + d_{roy} \end{bmatrix}$$
(11)

The parameters are defined as:

$$a_{1} = \frac{(j_{yy} - j_{zz})}{j_{xx}}, \quad a_{2} = \frac{j_{r}}{j_{xx}}, \quad a_{3} = \frac{(j_{zz} - j_{xx})}{j_{yy}}$$
$$a_{4} = \frac{j_{r}}{j_{yy}}, \quad a_{5} = \frac{(j_{xx} - j_{yy})}{j_{zz}}$$
$$b_{\Phi} = \frac{l}{j_{xx}}, \quad b_{\theta} = \frac{l}{j_{yy}}, \quad b_{\psi} = \frac{1}{j_{zz}}$$
$$\delta_{x} = \sin(\theta)\cos(\Phi)\cos(\psi) + \sin(\Phi)\sin(\psi),$$
$$\delta_{y} = \sin(\theta)\cos(\Phi)\cos(\psi) - \sin(\Phi)\sin(\psi),$$

$$\delta_z = \cos(\theta) \cos(\Phi)$$

The block diagram scheme of the controller is shown in Figure. 3.

Factors considered for designing a controller are

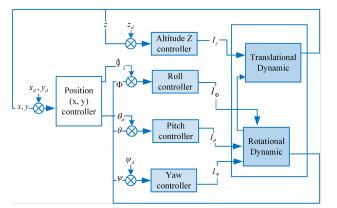


Figure 3. Controller Scheme diagram of the quadcopter

simple, robust, and provide good tracking performance without requiring information on the top range of the disturbances. The general sliding mode control law is:

$$I_i^+ = I_{eqvi} + I_{si} \tag{12}$$

 I_{eqvi} is the input/output linearization and I_{si} is the switching control law, which provides additional control effort to minimize tracking errors and the effect of disturbances.

3.1 Design a proportional-fractional order-integral-derivative sliding surface sliding mode control with backstepping

For choice of sliding surface procedure; tracking error (e_i) for SMC with BS [Bouabdallah and Siegwart, 2005] is;

$$e_i = x_{id} - x_i, \quad i \in \{1, 3, 5, 7, 9, 11\}$$

$$\dot{e}_i = \dot{x}_i - \dot{x}_{(i-1d)} - \gamma_{(i-1)} e_{(i-1)}, \quad i \in \{2, 4, 6, 8, 10, 12\}$$

$$\ddot{e}_i = \dot{x}_2 - \ddot{x}_{1d} - \gamma_1 \dot{e}_1 \quad \text{with } 0 < \gamma_i < \infty \quad (13)$$

Considering the Lyapunov function is:

$$V_{i} = \frac{1}{2}e_{i}^{2}, \quad i \in \{1, 3, 5, 7, 9, 11\}$$
$$V_{i} = \frac{1}{2}(s_{(i-1)} + e_{i}^{2}), \quad i \in \{2, 4, 6, 8, 10, 12\}$$
(14)

These satisfy the necessary sliding condition $\dot{S} < 0$. Let's take the PFOID as a sliding surface, and its equation is based on the literature [Mian and Daobo, 2008],[Saini and Ohri, 2023]. The first-order equation of the PID sliding surface is:

$$\ddot{s}_i + \eta_i \dot{s}_i = k_{p_i} \dot{e}_i + k_{i_i} e_i + k_{d_i} \ddot{e}_i, \quad \eta_i \in \mathbb{R}^+$$

Convert into the form of PFOID (with the second derivate);

$$\ddot{s}_i + \eta_i \dot{s}_i = k_{p_i} \dot{e}_i + k_{i_i}^{\mu} e_i + k_{d_i}^{\sigma} \ddot{e}_i \qquad (15)$$

Here, $I_i = \{i = (2 = \Phi, 4 = \theta, 6 = \psi)\}$ is the control input for the rotational subsystem, and $I_i = \{i = (8 = z, 10 = x, 12 = y)\}$ is the control input for the translational subsystem of the quadcopter.

Calculation for roll:

Let i=1,2 Surface are;

$$e_1 = x_{1d} - x_1$$

$$S_2 = e_2 = x_2 - \dot{x}_{1d} - \gamma_1 e_1 \tag{16}$$

and Lyapunov function is;

$$V(e_1, S_2) = \frac{1}{2} \left(e_1^2 + S_2^2 \right)$$

Applying the condition $SS \leq 0$ for the surface, makes the following:

$$\dot{s}_2 = -\beta_1 \operatorname{sign}(s_2) - \alpha_2 s_2$$

= $\dot{x}_2 - \ddot{x}_{1d} - \gamma_1 \dot{e}_1$
= $a_1 \dot{\theta} \dot{\psi} + a_2 \ddot{\theta} \Omega_r + b_\Phi I_\Phi + d_{ro\Phi} - \ddot{x}_{1d} - \gamma_1 (e_2 + \gamma_1 e_2)$
(17)

Converting eq. (14) in terms of roll;

$$\ddot{s}_2 + \eta_{\Phi} \dot{s}_2 = k_{p\Phi} \dot{e}_2 + k_{i\Phi}^{\mu} e_2 + k_{d\Phi}^{\sigma} \ddot{e}_2 \qquad (18)$$

Using the eq. (17) and put the value of \ddot{e}_2 from (10) and (16);

$$\begin{split} \ddot{s}_{2} + \eta_{\Phi} \dot{s}_{2} &= \\ k_{p\Phi} \dot{e}_{2} + k_{i\Phi}^{\mu} e_{2} + k_{d\Phi}^{\sigma} \left(a_{1} \dot{\theta} \dot{\psi} + a_{2} \ddot{\theta} \Omega_{r} \right. \\ &+ b_{\Phi} I_{\Phi} + d_{ro\Phi} - \ddot{x}_{1d} - \gamma_{1} (e_{2} + \gamma_{1} e_{2})) \end{split}$$
(19)

For the essential condition $\ddot{s}_2 = 0$, for tracking error to remain on the sliding surface and external disturbance is zero $d_{ro\Phi} = 0$;

$$I_{\Phi} = \frac{1}{b_{\Phi}k_{d\Phi}^{\sigma}} \left(-\eta_{\Phi}\dot{s}_{2} + k_{p\Phi}\dot{e}_{2} + k_{i\Phi}^{\mu}e_{2} + k_{d\Phi}^{\sigma}\left(a_{1}\dot{\theta}\dot{\psi} + a_{2}\ddot{\theta}\Omega_{r} - \ddot{x}_{1d} - \gamma_{1}(e_{2} + \gamma_{1}e_{2})\right)$$

$$\tag{20}$$

Now added the disturbance and the switching function [Fang et al., 2010] in eq. (19);

$$I_{\Phi} = \frac{1}{b_{\Phi}k_{d\Phi}^{\sigma}} \left(-\eta_{\Phi}\dot{s}_{2} + k_{p\Phi}\dot{e}_{2} + k_{i\Phi}^{\mu}e_{2} + k_{d\Phi}^{\sigma}\left(a_{1}\dot{\theta}\dot{\psi} + a_{2}\ddot{\theta}\Omega_{r} + d_{ro\Phi} - \ddot{x}_{1d} - \gamma_{1}(e_{2} + \gamma_{1}e_{1}) + (-\beta_{1}\text{sign}(s_{2}) - \alpha_{2}s_{2})\right)$$
(21)

 \ddot{s}_2 is calculated by substituting eq. (20) in (19)

$$\ddot{s}_{2} = -k_{d\Phi}^{\sigma}d_{ro\Phi} - b_{\Phi}k_{d\Phi}^{\sigma}\alpha_{2}s_{2} - b_{\Phi}k_{d\Phi}^{\sigma}\beta_{1}\operatorname{sign}(s_{2})$$
(22)
Converting, \ddot{s}_{2} into the generalization from \ddot{s}_{i} , for i
= 2, 4, 6, 8, 10, 12;

$$\ddot{s}_i = -k_{di}^{\sigma} d_{ro_i} - b_i k_{di}^{\sigma} \alpha_i s_i - b_i k_{di}^{\sigma} \beta_i \operatorname{sign}(\dot{s}_i)$$
(23)

where

$$\operatorname{sign}(\dot{s}(t)) = \begin{cases} +1, & \operatorname{if} \dot{s}(t) > 0\\ 0, & \operatorname{if} \dot{s}(t) = 0\\ -1, & \operatorname{if} \dot{s}(t) < 0 \end{cases}$$

Then modified eq. (22) with the disturbance;

$$I_{\Phi}^{+} = \frac{1}{b_{\Phi}k_{d\Phi}^{\sigma}} \begin{pmatrix} -\eta_{\Phi}\dot{s}_{2} + k_{p}\Phi\dot{e}_{2} + k_{i\mu}^{\mu}e_{2} \\ a_{1}\dot{\theta}\dot{\psi} + a_{2}\ddot{\theta}\Omega_{r} - \ddot{x}_{1d} \\ + d_{ro\Phi} - \gamma_{1} \\ (\dot{e}_{2} + \gamma_{1}e_{1}) \\ -\beta_{1}\operatorname{sign}(s_{2}) - \alpha_{2}s_{2} \end{pmatrix}$$
(24)

Other control inputs for rotational and translational subsystems are calculated on the same lines and are defined as;

$$I_{\theta}^{+} = \frac{1}{b_{\theta}k_{d\theta}^{\sigma}} \begin{pmatrix} -\eta_{\theta}\dot{s}_{3} + k_{p\theta}\dot{e}_{4} + k_{i\theta}^{\mu}e_{4} \\ a_{3}\dot{\psi}\dot{\Phi} + a_{4}\ddot{\Phi}\Omega_{r} - \ddot{x}_{3d} \\ +d_{ro\theta} - \gamma_{2} \\ (e_{4} + \gamma_{2}e_{3}) \\ -\beta_{3}\operatorname{sign}(s_{3}) - \alpha_{4}s_{3} \end{pmatrix}$$

$$(25)$$

$$I_{\psi}^{+} = \frac{1}{b_{\psi}k_{d\psi}^{\sigma}} \begin{pmatrix} \eta_{\psi}e_{4} + \eta_{\psi}e_{6} + \eta_{i\psi}e_{6} \\ + k_{d\psi}^{\sigma} \begin{pmatrix} a_{5}\dot{\Phi}(\dot{\theta}) - \ddot{x}_{5d} \\ + d_{ro\psi} - \gamma_{3} \\ (e_{6} + \gamma_{3}e_{5}) \\ -\beta_{5}\operatorname{sign}(s_{4}) - \alpha_{6}s_{4} \end{pmatrix}$$
(26)

3.2 Stability Interpretation

Theorem 1: In the paper, the sliding surface is defined by equation (22) and the control law I_{Φ} , I_{θ} , I_{ψ} , I_z is defined by equations (23), (24), (25), and (26). The system is asymptotically stable if $\dot{V}_i < 0$ (i.e., it is negative definite). For a positive definite differential quadratic Lyapunov function [Kumar and Dewan, 2023] defined as:

$$V_{i} = \frac{1}{2}s_{i}^{2} + \frac{1}{2}\dot{s}_{i}^{2} \text{ with} \begin{cases} V_{i}(0) = 0 \\ V(t) > 0 \text{ for } s_{i} \to (i = 2, 3, 4) \end{cases}$$
(27)

Proof 1: For roll, pitch, and yaw

Differentiating eq. (29) w.r.t time and substituting (22)

$$V_i = s_i \dot{s}_i + \dot{s}_i \ddot{s}_i \tag{28}$$

$$\dot{V}_i = s_i \dot{s}_i + \dot{s}_i \left(-k_i^{\sigma} d_{r_{oi}} - b_i k_i^{\sigma} \alpha_i s_i - b_i k_i^{\sigma} \beta_i \operatorname{sign}(\dot{s}_i) \right)$$

$$\dot{V}_i = \dot{s}_i \left(s_i - k_i^{\sigma} d_{r_{oi}} - b_i k_i^{\sigma} \alpha_i s_i - b_i k_i^{\sigma} \beta_i \operatorname{sign} |\dot{s}_i| \right)$$

$$\dot{V}_i \le |\dot{s}_i| \left(s_i - k_i^\sigma d_{r_{oi}} - b_i k_i^\sigma \alpha_i s_i - b_i k_i^\sigma \beta_i |\dot{s}_i| \right)$$

$$\dot{V}_{i} \leq \left|\dot{s}_{i}\right| \left(s_{i}\left(1 - b_{i}k_{i}^{\sigma}\alpha_{i}\right) + k_{i}^{\sigma}\left(d_{r_{oi}}^{+} - b_{i}\beta_{i}\right)\left|\dot{s}_{i}\right|\right)$$

Where $d_{r_{oi}}^+ \in \mathbb{R}^+$ is the upper bound on disturbance [Thanh and Hong, 2018]. For asymptotic stability, $\dot{V}_i < 0$;

 \dot{V}_i will always be negative if:

$$\begin{cases} \alpha_i > \frac{1}{b_i k_{di}^{\sigma}}, & \alpha_i \text{ for } i = 2, 4, 6\\ \beta_i > \frac{d_{r_{oi}}^+}{b_i}, & \beta_i \text{ for } i = 1, 3, 5 \end{cases}$$
(29)

Proof 2: for z

Using the eq. (22) and put the value \ddot{s}_5 that is found out by taking the same approach as \ddot{s}_2 , that is;

$$\ddot{s}_5 = -k_{dz}^{\sigma} d_{trz} - k_{dz}^{\sigma} \alpha_z s_5 - k_{dz}^{\sigma} \beta_7 \operatorname{sign}(\dot{s}_5)$$

Now,

$$\dot{V}_i = s_5 \dot{s}_5 + \dot{s}_5 \ddot{s}_5$$

$$\dot{V}_{i} = s_{5}\dot{s}_{5} + \dot{s}_{5}\left(-k_{dz}^{\sigma}d_{trz} - k_{dz}^{\sigma}\alpha_{8}s_{5} - k_{dz}^{\sigma}\beta_{7}\operatorname{sign}(\dot{s}_{5})\right)$$

$$V_{i} = \dot{s}_{5} \left(s_{5} - k_{dz}^{\sigma} d_{trz} - k_{dz}^{\sigma} \alpha_{8} s_{5} - k_{dz}^{\sigma} \beta_{7} |\dot{s}_{5}| \right)$$

$$\dot{V}_i \le |\dot{s}_5| \left(s_5 - k_{dz}^{\sigma} \alpha_8 s_5 - k_{dz}^{\sigma} d_{trz} - k_{dz}^{\sigma} \beta_7 |\dot{s}_5|\right)$$

$$\dot{V}_{i} \leq |\dot{s}_{5}| \left(s_{5} \left(1 - k_{dz}^{\sigma} \alpha_{8} \right) + k_{dz}^{\sigma} \left(d_{trz}^{+} - \beta_{7} \right) |\dot{s}_{5}| \right)$$

Where $d_{trz}^+ \in \mathbb{R}^+$ is the upper bound of disturbance. For asymptotic stability, $\dot{V}_i < 0$, and \dot{V}_i will always be negative if:

$$\begin{cases} \alpha_8 > \frac{1}{k} \frac{\sigma}{dz} \\ \beta_7 > d_{trz}^+ \end{cases}$$
(30)

Given that V_i is negative definite, all system state trajectories will converge to and remain on the corresponding sliding surfaces under the specified control laws.

4 Simulation results and discussion

The effectiveness and strength of the proposed controller (PFOID surface-based SMCBS) for attitude, altitude, and position control under external disturbances, ground effects, and payload are discussed in this section. Physical parameter values of the quadcopter are given in Table 1. The sliding gains were determined by the hit-and-trail method and the gain of the PID controller by the ultimate gain method (Table 2).

The total time interval (T) of the tracking trajectory of the quadcopter is from 0 to 35 seconds. The quadcopter traveling time has been divided into three intervals, as shown in Figure 3.

- 1. T_1 (0-15 seconds), a fixed point at 1.0 m height for hover state.
- 2. T₂ (15-25 seconds), the quadcopter lands from 1.0 m to 0.2 m.
- 3. T_3 (25-35 seconds), the quadcopter returns to a hover state at 1.2 m.

Aerodynamic drag, random noise, external disturbances, wind effects, ground effects, and mass variation due to payload discussed in Section 2 have been taken into account dynamically. The ground effect is significant only during the low-altitude flight of the vehicle (< 5R = 0.375, Figure 2). The landing set point is chosen < 0.2 m

Variable	Definition	х	у	Z	ϕ	θ	ψ
k_p	Proportional	4.9	4.9	11.0	8.0	8.0	8.0
k_i	Integral	0.68	0.68	1.01	1.33	1.44	0.89
k_d	Derivative	0.66	0.66	0.14	0.33	0.33	0.11
η	Constant Surface	2.0	2.0	2.0	1.0	1.0	3.0
α	Sliding Function	20.0	20.0	20.0	17.0	17.0	20.0
β	Shung Function	3.69	3.69	3.69	2.56	2.56	3.20
μ	Fractional order	0.8	0.8	0.8	0.8	0.8	0.8
σ		0.64	0.64	0.64	0.64	0.64	0.64

1.5

- - SMCBS

Table 2. Controller Parameters

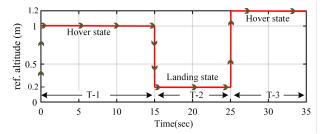
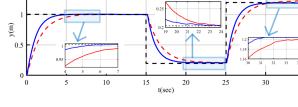


Figure 4. Reference Trajectory



PFOIDSMCBS - - - Reference

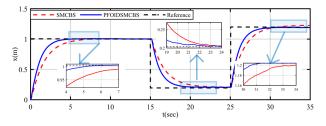
4.1 SIMULATION RESULTS

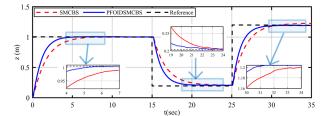
Simulation has been done for two scenarios.

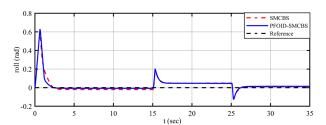
Scenario 1: Flight tracking under disturbances, wind, and ground effect.

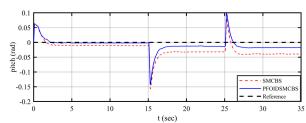
Scenario 2: Flight tracking under disturbances, wind and ground effect, and payload.

Scenario 1: During the first time interval, T-1; Quadcopter takes off from 0.0 m to achieve the height of 1.0 m after receiving the command. Ground effect is effective up to 5R=0.375. It tends to increase the rise time. The quadcopter reaches the desired altitude after 5.11 seconds in the case of the proposed controller and SMCBS controllers reach at 6.98 seconds. In T-2, the quadcopter lands at 0.2 m above the ground surface with the impact of the ground effect. The time taken by the proposed controller is 6.31 seconds, and SMCBS controllers are 8.14 seconds.









35

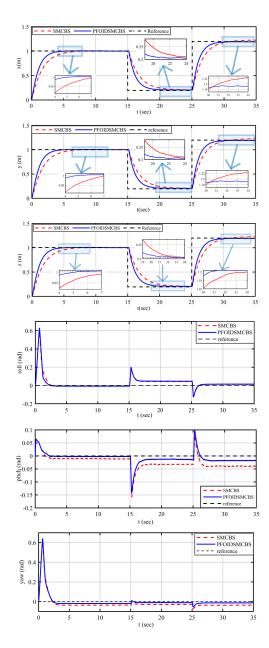


Figure 6. Performance comparison of the PFOIDSMCBS controller to SMCBS with various disturbances, wind effect, ground effect, and payload

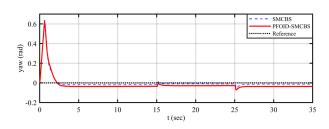


Figure 5. Performance comparison of the PFOIDSMCBS controller to SMCBS with various disturbances, wind effect, and ground effect

The quadcopter goes to a hover state from 0.2 m to 1.2

m in T-3 (t=25 to 35 seconds). SMCBS controllers take 8.44 seconds and proposed PFOIDSMCBS controllers take 5.32 seconds to complete the task. Performances specification for Figure 5 are quantified in Table 3. Performance has certainly improved by PFOIDSMCBS and the system is stable also as it satisfies stability criteria Table 6.

Scenario 2: This scenario is created based on the quadcopter's real-time applications. Considering, the quadcopter takes off with the payload (e.g. pesticide spray for agriculture) and sprays on the farm. After spraying, the quadcopter again goes to its original position. The other way around, the quadcopter lands on the ground picks up the payload, and returns to its position.

In case, (i) the quadcopter takes off with the payload (considering a +20% mass variation of the quadcopter), (ii) lands at 0.2 m near the field to spray, between 20 to 25 seconds, and then takes off without payload. From Figure. 6, in T-1, the quadcopter takes off from 0.0 m to achieve the height of 1.0 m with a +20% payload. The quadcopter reaches the desired altitude after 5.66 seconds in the case of the proposed controller and in the SMCBS controllers reaches 7.66 seconds. In T-2, the quadcopter lands at 0.2 m above the ground surface. Between 15 to 25 seconds, the quadcopter releases the payload slightly (in the agriculture spray process or parcel release process, etc.). The time taken by the proposed controller is 6.82 seconds, and the SMCBS controllers take 8.70 seconds.

The quadcopter goes to a hover state from 0.2 m to 1.2 m in T-3 (t = 25 to 35 seconds) with actual mass. SMCBS controllers take 8.24 seconds and proposed PFOIDSMCBS controllers take 5.22 seconds to complete the task. Performance specifications are quantified for Figure 6 in Table 4. Performance has certainly been improved by PFOIDSMCBS, and the system is stable also as it satisfies the stability criteria in Table 6.

From Table 3, it can be observed that the proposed controller during the landing state (time interval T-2) reduces the settling time by 6.12% as compared to the SMCBS of the system under no load. Additionally, the load is reduced by 5.17% from Table 4, in the z-direction.

From Figure 7, it is indicated that the proposed controller reduces chattering compared to the SMCBS controller. The proposed controller also requires less thrust during the quadcopter's hovering phase, indicating that it requires less control effort than the existing controller.

The proposed controller demonstrates performance in path tracking when compared to the existing SMCBS controller, even with a disturbed environment. Stability criteria are fulfilled according the eq. 31 and 32 from

Parameters	Controllers	Time Interval (sec)	Variables					
T at anicters	Controners		х	у	Z	ϕ	θ	ψ
Rise time	SMCBS	T-1 (0-15)	3.78	3.78	4.10	2.65	1.67	2.28
Kise time	PFOIDSMCBS	T-1 (0-15)	2.60	2.60	3.38	2.58	2.25	2.38
		T-1 (0-15)	0	0	0	0.61	0.06	0.610
	SMCBS	T-2 (15-25)	0	0	0	0.199	-0.155	-0.011
Overshoot Time		T-3 (25-35)	0	0	0	-0.120	0.08	-0.066
Overshoot Time	PFOIDSMCBS	T-1 (0-15)	0	0	0	0.68	0.06	0.63
		T-2 (15-25)	0	0	0	0.199	-0.141	0.009
		T-3 (25-35)	0	0	0	-0.120	0.11	-0.046
Settling Time	SMCBS	T-1 (0-15)	7.42	7.92	7.98	2.65	1.67	2.18
		T-2 (15-25)	22.66	22.66	22.7	16.94	17.92	16.13
		T-3 (25-35)	32.94	32.94	33.24	26.23	25.83	26.82
	PFOIDSMCBS	T-1 (0-15)	5.01	5.01	5.11	2.65	2.15	2.18
		T-2 (15-25)	21.20	21.20	21.31	16.94	17.64	16.13
		T-3 (25-35)	29.82	29.82	30.32	26.23	25.83	26.12
		T-1 (0-15)	0.001	0.001	0.001	-0.007	-0.009	-0.035
Steady State Error	SMCBS	T-2 (15-25)	0.002	0.002	0.003	0.04	-0.032	-0.020
		T-3 (25-35)	0.002	0.002	0.004	0.0143	-0.038	-0.036
		T-1 (0-15)	0.004	0.004	0.004	-0.007	-0.002	-0.033
	PFOID	T-2 (15-25)	0.002	0.002	0.002	0.044	-0.011	-0.009
	SMCBS	T-3 (25-35)	0.006	0.006	0.006	0.0143	-0.018	-0.066

Table 3. Performance specifications of the controller with various disturbances, wind effect, ground effect and no payload

Table 6; hence the system is asymptotically stable. According to the control law, every trajectory of the system's state will reach and stay on its designated sliding surface.

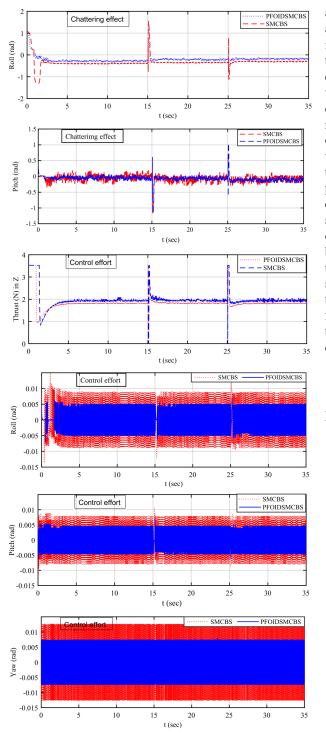


Figure 7. Chattering effect and control efforts

5 Conclusions

The paper proposed a hybrid controller (PFOIDSM-CBS) for stabilizing the quadcopter to follow the predefined trajectory. To attain the robustness of the proposed controller; deployed in various disturbances (external disturbances, ground effect, wind effect, and mass variation) during takeoff, inflight, and landing and

also compared with the existing controllers SMCBS and meets the stability requirements. Furthermore, in this study trajectory has been planned based on the quadcopters used in real-time applications. The quadcopter takes off to carry the payload (e.g., parcel, water or pesticide spray for agriculture, etc.) and drops/releases the payload to the ground. After the released payload, the quadcopter again goes to its original position. Respectively, the quadcopter takes off without the payload and lands on the ground. During to land quadcopter carries the load and returns to its position. The modelling outcomes demonstrate the effectiveness of the proposed controller in ensuring a soft landing for the quadcopter by mitigating the impact of thrust due to the ground effect. The wind deflected by the rotors near the ground generates extra thrust for the system, amending its planned trajectory to ensure a smooth landing. The controller successfully tracks the trajectory and achieves landing within a specified time frame, with no overshoot or undershoot. In the future, the proposed work could prove valuable for real-time drone missions.

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Number is a section of the interiment of t	Parameters	Controllers	Time Interval (sec)	Variables						
PFOID SMCBS T-1 (0-15) 2.40 2.40 2.53 2.58 2.25 2.38 Overshoot Time SMCBS T-1 (0-15) 0 0 0 0.61 0.06 0.610 T-2 (15-25) 0 0 0 0.119 -0.166 -0.011 T-3 (25-35) 0 0 0 0.199 -0.166 -0.011 T-2 (15-25) 0 0 0 0 0.68 0.060 0.63 PFOID SMCBS T-1 (0-15) 0 0 0 0.119 -0.122 0.011 T-2 (15-25) 0 0 0 0 0.68 0.66 0.63 T-2 (15-25) 0 0 0 0 0.119 -0.122 0.011 SMCBS T-1 (0-15) 7.36 7.36 7.66 2.65 1.67 2.18 T-2 (15-25) 22.89 23.01 17.91 18.39 16.99 T-3 (25-35) 32.94 32.94 33.24	i arameters	controners	Thire fifter var (See)	х	у	Z	ϕ	θ	ψ	
PFOID SMCBS T-1 (0-15) 2.40 2.40 2.53 2.58 2.25 2.38 Overshoot Time 5MCBS T-1 (0-15) 0 0 0 0.61 0.06 0.610 T-2 (15-25) 0 0 0 0.199 -0.166 -0.011 T-3 (25-35) 0 0 0 0.618 0.060 0.63 PFOID SMCBS T-1 (0-15) 0 0 0 0.1199 -0.122 0.011 F2 (15-25) 0 0 0 0 0.199 -0.122 0.011 SMCBS T-1 (0-15) 7.36 7.36 7.66 2.65 1.67 2.18 SMCBS T-2 (15-25) 22.89 23.01 17.91 18.39 16.99 T-3 (25-35) 32.94 32.94 33.24 26.23 25.83 26.82 PFOID SMCBS T-1 (0-15) 4.95 4.95 5.22 2.65 2.15 2.18 T-2 (15-25) 21.71 21.71 <th>Rise time</th> <td>SMCBS</td> <td>T-1 (0-15)</td> <td>3.67</td> <td>3.67</td> <td>3.96</td> <td>2.65</td> <td>1.67</td> <td>2.28</td>	R ise time	SMCBS	T-1 (0-15)	3.67	3.67	3.96	2.65	1.67	2.28	
SMCBS T-1 (0-15) 0 0 0 0.61 0.06 0.610 SMCBS T-2 (15-25) 0 0 0 0.199 -0.166 -0.011 T-3 (25-35) 0 0 0 0 0.61 0.061 -0.066 PFOID T-1 (0-15) 0 0 0 0.68 0.06 0.63 SMCBS T-2 (15-25) 0 0 0 0.199 -0.120 0.01 SMCBS T-2 (15-25) 0 0 0 0 0.110 -0.046 T-2 (15-25) 22.89 23.01 17.91 18.39 16.99 SMCBS T-1 (0-15) 7.36 7.36 7.66 2.65 1.67 2.18 T-2 (15-25) 22.89 23.91 17.91 18.39 16.99 SMCBS T-1 (0-15) 4.95 4.95 5.22 2.65 2.15 2.18 SMCBS T-1 (0-15) 0.001 0.001 0.001 0.0	Kise time	PFOID	T 1 (0 15)	2.40	2.40	2.53	2.58	2.25	2.38	
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Overshoot Time T-1 (0-15) 0 0 0 0.68 0.06 0.63 SMCBS T-2 (15-25) 0 0 0 0 0.199 -0.122 0.011 T-3 (25-35) 0 0 0 0 0 0.199 -0.122 0.011 T-3 (25-35) 0 0 0 0 0 0.110 -0.046 T-1 (0-15) 7.36 7.36 7.66 2.65 1.67 2.18 SMCBS T-2 (15-25) 22.89 23.01 17.91 18.39 16.99 T-3 (25-35) 32.94 32.94 33.24 26.23 25.83 26.82 PFOID T-1 (0-15) 4.95 4.95 5.22 2.65 2.15 2.18 T-2 (15-25) 21.71 21.71 21.82 17.91 18.23 17.49 SMCBS T-1 (0-15) 0.001 0.001 0.001 0.007 -0.036 -0.029 SMCBS T-1 (0-15) 0		SMCBS	T-2 (15-25)	0	0	0	0.199	-0.166	-0.011	
	Overshoot Time		T-3 (25-35)	0	0	0	-0.120	0.08	-0.066	
SMCBS T-2 (15-25) 0 0 0 0.199 -0.122 0.011 T-3 (25-35) 0 0 0 0 -0.120 0.11 -0.046 SMCBS T-1 (0-15) 7.36 7.36 7.66 2.65 1.67 2.18 SMCBS T-2 (15-25) 22.89 23.01 17.91 18.39 16.99 T-3 (25-35) 32.94 32.94 33.24 26.23 25.83 26.82 PFOID T-1 (0-15) 4.95 4.95 5.22 2.65 2.15 2.18 SMCBS T-2 (15-25) 21.71 21.71 21.82 17.91 18.39 16.99 SMCBS T-1 (0-15) 4.95 4.95 5.22 2.65 2.15 2.18 SMCBS T-2 (15-25) 21.71 21.71 21.82 17.91 18.23 17.49 SMCBS T-1 (0-15) 0.001 0.001 0.001 -0.007 -0.009 -0.035 T-2 (15-25)	Overshoot Time		T-1 (0-15)	0	0	0	0.68	0.06	0.63	
T-3 (25-35) 0 0 0 -0.120 0.11 -0.046 SMCBS T-1 (0-15) 7.36 7.36 7.66 2.65 1.67 2.18 SMCBS T-2 (15-25) 22.89 22.89 23.01 17.91 18.39 16.99 T-3 (25-35) 32.94 32.94 33.24 26.23 25.83 26.82 PFOID T-1 (0-15) 4.95 4.95 5.22 2.65 2.15 2.18 MCBS T-2 (15-25) 21.71 21.72 21.82 17.91 18.23 17.49 SMCBS T-3 (25-35) 29.82 29.82 30.32 26.23 25.83 26.12 Steady State Error SMCBS T-1 (0-15) 0.001 0.001 -0.007 -0.009 -0.035 Steady State Error SMCBS T-1 (0-15) 0.002 0.002 0.002 0.014 -0.036 -0.036 Steady State Error T-1 (0-15) 0.002 0.002 0.002 0.007 -0.002			T-2 (15-25)	0	0	0	0.199	-0.122	0.011	
SMCBS T-2 (15-25) 22.89 23.01 17.91 18.39 16.99 T-3 (25-35) 32.94 32.94 33.24 26.23 25.83 26.82 PFOID T-1 (0-15) 4.95 4.95 5.22 2.65 2.15 2.18 SMCBS T-2 (15-25) 21.71 21.71 21.82 17.91 18.23 17.49 SMCBS T-3 (25-35) 29.82 29.82 30.32 26.23 25.83 26.12 T-3 (25-35) 29.82 29.82 30.32 26.23 25.83 26.12 T-3 (25-35) 29.82 29.82 30.32 26.23 25.83 26.12 SMCBS T-1 (0-15) 0.001 0.001 0.001 -0.007 -0.009 -0.035 T-2 (15-25) 0.002 0.002 0.002 0.002 0.004 -0.007 -0.036 -0.036 T-1 (0-15) 0.004 0.004 0.004 -0.007 -0.002 -0.033 FC10D T-			T-3 (25-35)	0	0	0	-0.120	0.11	-0.046	
Settling Time T-1 (0-15) 32.94 32.94 33.24 26.23 25.83 26.82 PFOID SMCBS T-1 (0-15) 4.95 4.95 5.22 2.65 2.15 2.18 T-2 (15-25) 21.71 21.71 21.82 17.91 18.23 17.49 T-3 (25-35) 29.82 29.82 30.32 26.23 25.83 26.12 T-3 (25-35) 29.82 29.82 30.32 26.23 25.83 26.12 T-1 (0-15) 0.001 0.001 0.001 -0.007 -0.009 -0.035 Steady State Error SMCBS T-1 (0-15) 0.002 0.002 0.002 0.047 -0.036 -0.029 T-3 (25-35) 0.002 0.002 0.002 0.004 -0.007 -0.002 -0.036 PFOID T-1 (0-15) 0.004 0.004 0.004 -0.007 -0.002 -0.033 PFOID T-1 (0-15) 0.002 0.002 0.002 0.047 -0.022 -0.099		SMCBS	T-1 (0-15)	7.36	7.36	7.66	2.65	1.67	2.18	
Settling Time T-1 (0-15) 4.95 4.95 5.22 2.65 2.15 2.18 MCBS T-2 (15-25) 21.71 21.71 21.82 17.91 18.23 17.49 SMCBS T-3 (25-35) 29.82 29.82 30.32 26.23 25.83 26.12 SMCBS T-1 (0-15) 0.001 0.001 0.001 -0.007 -0.009 -0.035 SMCBS T-2 (15-25) 0.002 0.002 0.002 0.047 -0.036 -0.029 T-3 (25-35) 0.004 0.004 -0.007 -0.002 -0.033 FFOID T-1 (0-15) 0.002 0.002 0.004 -0.007 -0.002 -0.033 SMCBS T-1 (0-15) 0.004 0.004 -0.007 -0.002 -0.033 PFOID T-1 (0-15) 0.002 0.002 0.002 0.047 -0.022 -0.033 SMCBS T-2 (15-25) 0.002 0.002 0.047 -0.022 -0.099			T-2 (15-25)	22.89	22.89	23.01	17.91	18.39	16.99	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Settling Time		T-3 (25-35)	32.94	32.94	33.24	26.23	25.83	26.82	
SMCBS T-2 (15-25) 21.71 21.71 21.82 17.91 18.23 17.49 T-3 (25-35) 29.82 29.82 30.32 26.23 25.83 26.12 SMCBS T-1 (0-15) 0.001 0.001 0.001 -0.007 -0.009 -0.035 Steady State Error T-2 (15-25) 0.002 0.002 0.002 0.0143 -0.036 -0.029 T-3 (25-35) 0.002 0.002 0.002 0.002 0.0143 -0.038 -0.036 PFOID T-1 (0-15) 0.004 0.004 0.004 -0.007 -0.002 -0.033 SMCBS T-2 (15-25) 0.002 0.002 0.047 -0.022 -0.033	Setting Thie		T-1 (0-15)	4.95	4.95	5.22	2.65	2.15	2.18	
T-3 (25-35) 29.82 29.82 30.32 26.23 25.83 26.12 T-1 (0-15) 0.001 0.001 0.001 -0.007 -0.009 -0.035 Steady State Error T-2 (15-25) 0.002 0.002 0.002 0.004 -0.036 -0.029 F-3 (25-35) 0.002 0.002 0.002 0.002 0.0143 -0.038 -0.036 PFOID T-1 (0-15) 0.004 0.004 -0.007 -0.002 -0.033 SMCBS T-2 (15-25) 0.002 0.002 0.004 -0.007 -0.002 -0.033			T-2 (15-25)	21.71	21.71	21.82	17.91	18.23	17.49	
Steady State Error SMCBS T-2 (15-25) 0.002 0.002 0.002 0.002 0.0047 -0.036 -0.029 Fr3 (25-35) 0.002 0.002 0.002 0.002 0.002 0.0143 -0.038 -0.036 PFOID T-1 (0-15) 0.004 0.004 0.004 -0.007 -0.002 -0.033 SMCBS T-2 (15-25) 0.002 0.002 0.002 0.047 -0.022 -0.099			T-3 (25-35)	29.82	29.82	30.32	26.23	25.83	26.12	
Steady State Error T-3 (25-35) 0.002 0.002 0.002 0.0143 -0.038 -0.036 PFOID T-1 (0-15) 0.004 0.004 0.004 -0.007 -0.002 -0.033 SMCBS T-2 (15-25) 0.002 0.002 0.002 0.047 -0.022 -0.099		SMCBS	T-1 (0-15)	0.001	0.001	0.001	-0.007	-0.009	-0.035	
Steady State Error T-1 (0-15) 0.004 0.004 0.004 -0.007 -0.002 -0.033 PFOID T-2 (15-25) 0.002 0.002 0.002 0.047 -0.022 -0.099	Steady State Error		T-2 (15-25)	0.002	0.002	0.002	0.047	-0.036	-0.029	
PFOID T-1 (0-15) 0.004 0.004 0.004 -0.007 -0.002 -0.033 SMCBS T-2 (15-25) 0.002 0.002 0.002 0.047 -0.022 -0.099			T-3 (25-35)	0.002	0.002	0.002	0.0143	-0.038	-0.036	
SMCBS <u>T-2 (15-25)</u> 0.002 0.002 0.002 0.047 -0.022 -0.099			T-1 (0-15)	0.004	0.004	0.004	-0.007	-0.002	-0.033	
T-3 (25-35) 0.006 0.006 0.006 0.0143 -0.018 -0.066			T-2 (15-25)	0.002	0.002	0.002	0.047	-0.022	-0.099	
			T-3 (25-35)	0.006	0.006	0.006	0.0143	-0.018	-0.066	

Table 4. Performance specifications of the controller under various disturbances, mass variation, ground control, and payload

Table 5. Stability Analysis

Parameter values	$\alpha_2 = 20$	$\alpha_4 = 20$	$\alpha_6 = 20$	$\alpha_8 = 20$	$\beta_1 = 2.56$	$\beta_3 = 3.20$	$\beta_5 = 3.20$	$\beta_7 = 3.69$
Parameter values	$\frac{1}{b_{\phi}k\sigma d_{\phi}} = 3.78$	$\frac{1}{b_{\theta}k\sigma} = 3.78$	$\frac{1}{b_{\psi}k\sigma d_{\psi}} = 5.56$	$\frac{1}{k\sigma d_z} = 1.25$	$\frac{d_{r\phi}^+}{b_{\phi}} = 0.71$	$\frac{d_{r\theta}^+}{b_{\theta}} = 0.57$	$\frac{d_{r\psi}^+}{b_{\psi}} = 2.35$	$d_{trz}^+ = 1.67$

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