

# Investigation of Self-Fields Effects on Dispersion Relation in a Helical Wiggler with Ion-Channel Guiding

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It is known that the self-electric and self-magnetic fields induced by charge and current densities of the electron beam have significant effects on the operation of a free-electron laser<sup>1</sup>. Recently, more exact calculations of self-fields and analysis of their effects on electron dynamics and gain have been published<sup>2, 3</sup>. The purpose of this paper is to investigate the effects of self-fields on dispersion relation in a free-electron laser with helical wiggler and ion-channel guiding. A sixth degree polynomial dispersion equation showing coupling of electromagnetic and space-charge waves by the wiggler magnetic field is derived. Numerical solutions of the polynomial equation yield the complex wave number  $k$  as a function of the wave frequency  $\omega$ . These solutions are used to study growth rate. A numerical study of the growth rate in the presence of the self-fields is presented and compared with the growth rate in the absence of the self-fields. It is shown that for helical wiggler and ion-channel guiding the growth rate decreases due to the self-fields. The growth rate decrement increases with increasing electron beam density.

**Keywords:** *free-electron laser, dispersion relation, growth rate, and ion-channel guiding.*

## References:

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- <sup>2</sup>M. Esmailzadeh, J. E. Willett, and L. J. Willett, *J. Plasma Phys.* **72**, 59 (2006).
- <sup>3</sup>M. Esmailzadeh and J. E. Willett, “*Self-fields effects on gain in a free-electron laser with helical wiggler and axial magnetic field*” to be published in *Phys. Plasmas*.